

Unequal wages for equal utilities¹

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Abstract

In a society where individuals only differ in productivity the *laissez-faire* distribution of utilities is closely linked to that of productivity. From a utilitarian viewpoint the ideal distribution of productivity is the most equal one. Does this proposition still hold if one can redistribute income? We show that in this case the most unequal distribution of productivity is that which implies the most equal distribution of utilities in the first-best. In the second-best, this conclusion holds under some plausible conditions.

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1 Introduction

One of the main rationales for public involvement in education is redistribution. In the literature, the design of an optimal educational policy is usually combined with that of a redistributive income tax. In that framework education is not the only channel of redistribution; there is also in a second stage an income tax that can alter social welfare. The government's problem is first to determine the amount and distribution of public education and then to design the structure of the income tax. The standard approach is to assume a population of individuals who differ in their ability to benefit from education. This heterogeneity typically implies a rather regressive distribution of public education: resources are concentrated on the most able individuals in order to get a "cake" as big as possible to share among individuals through income taxation; see e.g., Bruno (1976), Hare and Ulph (1979) and Ulph (1977). Note that this "perverse" distribution effect just mentioned is partially mitigated when we introduce decreasing returns of educational spending.¹Naturally, if we restrict the exercise to the first stage, the solution is also different and tends to be less regressive. This is shown for instance by Arrow (1971) who studies the optimal distribution of a given amount of public expenditure among individuals differing in their learning ability without accounting for the possibility of subsequent income redistribution.

In this paper we put forward another reason to push for regressive education. It is not linked to heterogeneity in innate ability to benefit from education but to pervasive non-convexities that arise in the optimal income tax problem when individual productivities are endogenous (depend on education). This point has been neglected so far.² To make it as clear as possible, we assume away differences in learning abilities, decreasing returns of education and we suppose that the total amount of public expenditure on education is given. We shall discuss the implications of those three assumptions in the concluding section.

¹Bovenberg and Jacobs (2005) and Maldonado (2007).

²Note however that it is implicitly acknowledged by Bovenberg and Jacobs (2005) who avoid it by making suitable assumptions on the education technology.

We show that when the general redistributive framework includes an education policy that determines the distribution of wage and an optimal income tax *à la Mirrlees*, then the most unequal distribution of wage happens to be desirable from the standpoint of social welfare maximization. In other words, in our setting, it is “more efficient” to redistribute incomes rather than to equalize wages.

This rather surprising and to some extent counter-intuitive result has to be interpreted with great care. It does have practical relevance because the effects that are at work in our simple setting (and the push for a corner solution) are also going to be relevant in much more complex (and realistic) frameworks. Consequently, the advocates of a progressive education policy have to show that there are benefits to wage equalization that outweigh the non-convexities we are putting forward. We shall revisit this issue in the concluding section. In the meantime let us just point out that our result is clearly at odds with the literature on equal opportunity that would recommend wage equality.³ In fact, we here have a trade-off between equal opportunity and utilitarian welfare maximization. It is also at odds with the observation that in many countries public spending in education, but also in health is more redistributive than income taxation. If such an observation is correct and if it is seen from the perspective of our results it suggests that effective income taxation is far from being optimal.

To keep our arguments as simple as possible, we use the two-ability version of Mirrlees (1972)’s model by Stiglitz (1982). Stiglitz studies the optimal income tax schedule where there is a fraction n_i of workers with productivity w_i ($i = 1, 2$). Traditionally, both (n_1, n_2) on the one hand and (w_1, w_2) are given. The only restriction is that $w_2 > w_1$. Recently there has been some attempts to study the incidence of a change in n_1/n_2 over the optimal tax schedule and the extent of redistribution.⁴ Yet there exist no study on the incidence of a change in w_1 and w_2 .

Suppose now that through its educational policy the government can choose

³Romer (1998), Athanasiou (2007).

⁴Boadway and Pestieau (2007).

the vector (w_1, w_2) subject to some constraint $n_1w_1 + n_2w_2 = a$ (constant to be specified below). This amounts to assuming the wages are determined by education expenditures through a linear technology and that the total education budget is given. The natural question to ask is what is the most desirable distribution of (w_1, w_2) given that whatever the vector (w_1, w_2) chosen there will be some redistributive taxation policy. At first glance, one is tempted to lean towards equal wages, $w_1 = w_2$. This appears to be the most “natural” solution at least with a concave social welfare function (when society cares for equality). Furthermore with equal wages, there is no need to resort to distortionary taxation to redistribute incomes. Consequently, a first-best policy is attainable.

We show in this paper that such an intuitive thinking is wrong and that the optimal distribution of abilities is the most unequal one. In the first-best, one easily shows that with quasi linear preferences individual utility is a *convex* function of w so that the equal wages solution is a local social welfare minimum. By endowing one type of individual with maximum ability we get more aggregate utility than by endowing both types with average ability. Second-order conditions are more complicated with general preferences but we provide a simple argument to show that wage differentiation always dominates wages equalization. All these results are obtained in a first-best setting, when there is no asymmetric information that hinders income distribution. When wages are not observable in the second stage one would expect the case for equal wages to be considerably strengthened. Quite surprisingly this turns out not to be the case. Specifically, we show that in a second-best setting, the most unequal distribution of productivity remains desirable if it implies zero productivity for all but one type. It is only when there is a positive “productivity floor” (implying an exogenous limit to wage differentiation), that an equal distribution of productivity *may* become desirable in a second-best setting.

The rest of this paper is organized as follows. After introducing the basic model, we first deal with the first-best setting (Section 3) and then with the second best-one (Section 4). In Section 5, we present a numerical example.

2 The economy

In the line of Stiglitz (1982) we consider two types of individuals $i = 1, 2$ with relative size $n_i > 0$ (so that $n_1 + n_2 = 1$) and identical utilities

$$u_i(x_i, \ell_i), \quad (1)$$

where x_i is consumption of a numeraire good and ℓ_i labor supply. Productivities (or wages) w_i are *endogenous* and satisfy what we call the educational technology. We characterize this technology through Γ the set of feasible wages that is defined by

$$\Gamma = \{(w_1, w_2) | n_1 w_1 + n_2 w_2 = 2 \text{ and } w_i \geq \underline{w}\} \text{ with } 1 \geq \underline{w} \geq 0. \quad (2)$$

In words we have a linear technology according to which earnings ability can be “transferred” between types on a one by one basis. To understand this formulation assume first that $\underline{w} = 0$. In that case the education technology has two extreme cases. One is the complete equalization of wages $w_1 = w_2 = 1$ and the other is the maximum wage inequality with say $w_1 = 0$ and $w_2 = 1/n_2$ where all educational resources are devoted to type 2 individuals. The role of \underline{w} is to limit the scope of wages inequalities that is feasible.

We specify the education technology in terms of wages to make the link to the optimal taxation literature. The formalization we use may appear somewhat unusual, but can be derived from a more conventional specification of the education technologies as it is often found in the literature. Following Ulph (1977) we can specify individual wages as $w_i = \phi_i(\theta_i, e_i)$, where θ_i is (exogenous) ability to benefit from educations and e_i is education expenditure. This is exactly equivalent to the technology we use if (i) individuals are identical ex ante (θ_i is the same for all), (ii) ϕ is linear in e_i (for instance $w_i = A e_i$ where A is some constant) and (iii) the total budget for education expenditures is fixed at E (so that $n_1 e_1 + n_2 e_2 = E$).⁵

⁵For instance, we would have $w_1 = \theta_1 e_1^\alpha$ and $w_2 = \theta_2 e_2^\alpha$ where $\theta_1 \neq \theta_2$ reflects different learning ability and $\alpha \leq 1$ implies decreasing returns. In our paper $e_1 + e_2 = 2$, $\alpha = 1$ and

To evaluate welfare, we adopt a symmetric social criterion:

$$W = \sum n_i \psi(u_i),$$

where $\psi(\cdot)$ is concave. An extreme form of $\psi(\cdot)$ yields the Rawlsian criterion:

$$W = \min[u_1, u_2].$$

For the remainder of the paper we assume for notational convenience and without loss of generality that $n_1 = n_2 = 1/2$.

3 First-best

3.1 General problem: statement

Assume full information and free use of lump-sum transfers. The optimal allocation is then determined by solving:

$$\max_{\ell_i, w_i, T_i} W = \Psi[u(w_1 \ell_1 - T_1, \ell_1)] + \Psi[u(w_2 \ell_2 - T_2, \ell_2)], \quad (3)$$

$$\text{s.t.} \quad w_1 + w_2 = 2, \quad (4)$$

$$T_1 + T_2 = 0 \quad (5)$$

$$w_i \geq \underline{w}. \quad (6)$$

This is similar to the standard first-best benchmark considered by Stiglitz (1982), except that we have endogenous wages. We concentrate on the first-order condition with respect to w_i . Substituting for $w_2 = 2 - w_1$ and differentiating yields

$$\frac{\partial W}{\partial w_1} = (\ell_1 - \ell_2)\lambda,$$

where $\lambda > 0$ is the Lagrange multiplier of the resource constraint (5). This FOC is always satisfied for $w_1 = w_2 = 1$ (along with $\ell_1 = \ell_2$) so that one might be tempted to think that the solution implies equalization of wages. However, we cannot simply assume that the SOC to be satisfied here. The SOC condition for the general problem (with 6 decision variables) is complicated but the potential for nonconvexities can be illustrated by considering a special case.

$\theta_1 = \theta_2 = 1$. To be more precise, this specification yields (2) with $\underline{w} = 0$. To generate a positive level of \underline{w} we would have to add a constraint specifying a minimum level of e_i .

3.2 Quasi-linear illustration

Assume quasi-linear preferences specified by $u_i(x_i, \ell_i) = x_i - v(\ell_i)$. With such preferences it is plain that Pareto efficiency requires the maximization of “surplus” given by

$$S = w_1 \ell_1 + w_2 \ell_2 - v(\ell_1) - v(\ell_2).$$

Furthermore individual labor supplies ℓ_i can be expressed solely as a function of w_i (there is no income effect). Substituting $w_2 = 2 - w_1$ we then reduce the problem to a single dimension and write $\tilde{S}(w_1)$. Differentiating yields

$$\frac{d\tilde{S}}{dw_1} = \ell_1(w_1) - \ell_2(2 - w_1), \quad (7)$$

$$\frac{d^2\tilde{S}}{dw_1^2} = \frac{d\ell_1}{dw_1} + \frac{d\ell_2}{dw_2} > 0, \quad (8)$$

which shows that $\tilde{S}(w_1)$ is a convex function. Consequently, with quasi-linear preferences equalization of wages is never optimal. Instead, we have a corner solution which involves “maximum differentiation”. Specifically, when it is feasible (i.e, when $\underline{w} = 0$) one individual will have a zero wage (and not work at all) while the other one will have a positive wage (namely $w_i = 2$) and labor supply. When $\underline{w} > 0$, this extreme solution is not feasible. However, it continues to be true that wages ought to be differentiated as much as possible.

To sum up, the maximal wage differentiation maximizes the size of total surplus and thus applies at all Pareto efficient allocations. When Ψ is strictly concave, social welfare is maximized when utilities are equalized. This is achieved through lump-sum transfers. Recall that we are in a first-best world for the time being so that redistribution (of incomes) does not involve any efficiency loss.

3.3 General problem: solution

With general preferences we can no longer reduce the problem to a single dimension and the SOCs are too complicated to be conclusive. However, we can use a different approach and directly compare the relevant levels of welfare, namely W^I

(achieved when $w_1 = w_2 = 1$) and W^C (achieved when, say, $w_1 = (2 - \underline{w})$ and $w_2 = \underline{w}$), and show that $W^C \geq W^I$ so that maximum differentiation continues to dominate even with general preferences).

To see this, define the level of labor supply under wage (and consumption) equalization

$$\ell^I = \arg \max_{\ell} \Psi [u(\ell, \ell)] + \Psi [u(\ell, \ell)]. \quad (9)$$

Maximum welfare is then given by

$$W^I = \Psi [u(\ell^I, \ell^I)] + \Psi [u(\ell^I, \ell^I)]. \quad (10)$$

At a corner solution with $w_1 = (2 - \underline{w})$ and $w_2 = \underline{w}$, maximum welfare is given by

$$W^C = \max_{\ell_1, \ell_2, T} \Psi [u(w_1 \ell_1 - T, \ell_1)] + \Psi [u(w_2 + T, \ell_2)] \quad (11)$$

where T is a lump-sum transfer. By setting T to equalize consumption levels (which is generally *not* the optimal level)⁶ we obtain

$$W^C \geq \max_{\ell_1, \ell_2} \Psi \left[u \left(\frac{w_1 \ell_1 + w_2 \ell_2}{2}, \ell_1 \right) \right] + \Psi \left[u \left(\frac{w_1 \ell_1 + w_2 \ell_2}{2}, \ell_2 \right) \right].$$

By setting $\ell_1 = \ell_2 = \ell^I$ (which is again generally not optimal) and using $w_1 = (2 - \underline{w})$ and $w_2 = \underline{w}$ we then obtain

$$W^C \geq \Psi [u(\ell^I, \ell^I)] + \Psi [u(\ell^I, \ell^I)] = W^I.$$

Consequently, the corner solution dominates because for $w_1 = (2 - \underline{w})$ and $w_2 = \underline{w}$ there are feasible choices of labor supplies and transfer which yield (at least) the same level of welfare as under wage equalization.

To sum up, we have the following proposition

Proposition 1 *Assume that preferences are represented by $u_i(x_i, \ell_i)$ and that wages can be chosen according to $w_1 + w_2 = 2$, with $w_i \geq \underline{w}$. When individual types are observable (so that personalized lump-sum transfers are available), the*

⁶Unless for instance Ψ is linear while u is strongly separable.

level of welfare achieved under maximum wage differentiation (with $w_i = \underline{w}$ and $w_j = 2 - \underline{w}$) is always at least as high as (and generally higher than) the level of welfare achieved under wage equalization (with $w_1 = w_2 = 1$).

In words, in a first-best setting, equalization of wages (according to the linear technology considered here) is at best useless and generally yields a reduction in welfare. Roughly speaking, the best strategy is thus to redistribute incomes rather than abilities. Recall that with the linear education technology considered, redistribution of abilities does not involve any efficiency loss per se (the total cake does not become smaller). Yet, it proves not to be desirable.

Even though this result may at first seem surprising, the intuition becomes obvious under closer scrutiny. Consider the simplest case with $\underline{w} = 0$. Then if we go from equal wages to wage $w_2 = 2$, individual 2's wage is effectively doubled. This means that we can produce the same output as under equal wages by having only one individual work. The proof of Proposition 1 is constructed around this argument (which becomes slightly more complicated when $\underline{w} > 0$).

4 The second-best

So far we have assumed full information under which redistribution of incomes through lump-sum taxes and transfers is possible and does not involve any efficiency loss (we move along the Pareto frontier). We now turn to a setting of symmetric information and assume that only income $y_i = w_i \ell_i$ is publicly observable, while wages and labor supplies are private information. This is the information structure on which most of the optimal tax literature is based. In this setting the case for equalization of wages appears to be considerably strengthened. Specifically, when wages are equalized, distortionary redistribution of incomes is not needed. Conversely, the maximal wage differentiation may, as shown in the previous section, yield a bigger “cake”, but it is not clear if it remains bigger once the efficiency losses of income redistribution are incurred.

Quite surprisingly, when $\underline{w} = 0$, maximal wage differentiation continues to dominate even in a second-best setting. We show this through two propositions. The first one is of limited scope and applies only to some classes of utility functions. However, it provides some interesting intuition. The second one applies to all utility functions but is established in a more indirect way.

To specify the second-best problem, we can start from the first-best problem, (3)–(6) to which we have to add the following two incentive constraints

$$u(x_i, \ell_i) \geq u(x_j, \tilde{\ell}_j) \quad i, j = 1, 2; i \neq j,$$

where $\tilde{\ell}_j = w_j \ell_j / w_i$ is the labor supply of individual i mimicking individual j . Observe that when $w_j \ell_j > 0$, $\tilde{\ell}_j$ is only defined if $w_i > 0$. An individual with zero wage can never mimick an individual with positive wage (and labor supply).

Now, assume $\underline{w} = 0$ and consider an allocation with maximum wage differentiation and say $w_1 = 0$ and $w_2 = 2$. Assume for the time being that the first-best allocation (solution to (3)–(6)) implies

$$u(x_2, \ell_2) \geq u(x_1, 0) \tag{12}$$

so that the productive individual (who works) has a utility level that is at least as high as that of the non productive individual (who does not work). In that case it is plain that the first-best solution is also the second-best solution. Put differently, the full information optimum remains implementable under asymmetric information. To see this note that (12) implies that the incentive constraint of type 2 individuals is satisfied because with $w_1 = 0$ we have $\tilde{\ell}_2 = \ell_1 = 0$.⁷ Furthermore with $w_1 = 0$ type 1 individuals cannot mimick type 2 individuals. We thus have the following proposition:

Proposition 2 *Assume $\underline{w} = 0$. When the first-best solution with $w_i = 0$ and $w_j = 2$ ($i, j = 1, 2; i \neq j$) implies $u(x_j, \ell_j) \geq u(x_i, 0)$, then it can also be implemented if individual incomes are observable while wages and labor supplies are not.*

⁷This is no longer true when $\underline{w} > 0$.

This proposition applies to a number of interesting settings. In particular, it holds for the Rawlsian welfare function or with quasi linear preferences when Ψ is linear (simple utilitarian criterion). However, there are also many instances where it does not apply. A prominent and well known example is the case of separable preferences $u(x, \ell) = f(x) - g(\ell)$, where the first-best implies $x_1 = x_2$ so that (12) is violated under maximum wage differentiation (the productive individual is worse off than the unproductive individual).

When Proposition 2 applies, the first-best solution can be implemented in the second-best. Consequently first and second best solutions coincide (and both imply maximum wage differentiation). When (12) is violated, the first-best solution can no longer be implemented in the second best. However, as long as $\underline{w} = 0$ we can show that maximum wage differentiation continues to dominate the solution with equal wages.

Recall that with equal wages the best solution is achieved with $x_i = \ell_i = \ell^I$, where ℓ^I is defined by (9). Since individuals are treated identically this is both a first- and a second best solution. Now consider again an allocation with maximum wage differentiation and say $w_1 = 0$ and $w_2 = 2$. Set $\ell_2 = \ell^I$ and define \widehat{T} such that

$$u(\widehat{T}, 0) = u(\ell^I, \ell^I). \quad (13)$$

Observe that $T < \ell^I$ (utility being decreasing in ℓ). It is then easy to verify that the allocation defined by $x_1 = \widehat{T}$, $\ell_1 = 0$, $x_2 = 2\ell^I - \widehat{T}$ and $\ell_2 = \ell^I$, is feasible, Pareto dominates the equal wage solution $x_i = \ell_i = \ell^I$ and is incentive compatible. Pareto dominance follows from (13) for individual 1. For individual 2, $\widehat{T} < \ell^I$ implies

$$u(x_2, \ell_2) = u(2\ell^I - \widehat{T}, \ell^I) > u(\ell^I, \ell^I). \quad (14)$$

Finally, combining (13) and (14) yields

$$u(x_2, \ell_2) > u(\widehat{T}, 0),$$

which implies incentive compatibility.⁸ To sum up, we have established the fol-

⁸To establish (14) one needs $w_2 = 2$ and thus $w_1 = 0$.

lowing proposition

Proposition 3 *Assume $\underline{w} = 0$. Under maximum wages differentiation with $w_i = 0$ and $w_j = 2$ ($i, j = 1, 2; i \neq j$) there exists a feasible allocation defined by $x_i = \widehat{T}$, $\ell_i = 0$, $x_j = 2\ell^I - \widehat{T}$ and $\ell_j = \ell^I$ (where \widehat{T} satisfies $u(\widehat{T}, 0) = u(\ell^I, \ell^I)$) that Pareto dominates the best equal wage solution ($x_i = \ell_i = \ell^I$), and is incentive compatible.*

The allocation we have constructed to establish this proposition is of course in general not the optimal one but this can only strengthen the case against wage equalization.

To sum up, as long as $\underline{w} = 0$, wage equalization is never optimal, even in the second-best (i.e., even when it makes potentially costly ex post redistribution unnecessary). However, it is also clear that the assumption $\underline{w} = 0$ plays a crucial role in the proofs to both propositions. This does not mean that the (second- best) results are reversed as soon as $\underline{w} > 0$. However, the dominance of maximum wage differentiation can then no longer be established at the same level of generality; we then can no longer rule out that wage equalization may be optimal in some situation. To illustrate this point we now turn to a numerical example.

5 Numerical example

To illustrate the argument at hand we use a quadratic disutility for labor so that in the *laissez-faire*:

$$u_i = w_i \ell_i - \ell_i^2 / 2 = w_i^2 / 2.$$

With such a specification we can represent social indifference curves in the plane (w_1, w_2) . Using a utilitarian social welfare function, we have:

$$S = \frac{w_1^2}{2} + \frac{w_2^2}{2}.$$

Consequently, social indifference curves are quarter circles as represented in Figure 1. When $w_1 + w_2 = 2$, we reach the same level $S = 2$ with $(w_1, w_2) = (2, 0)$ or

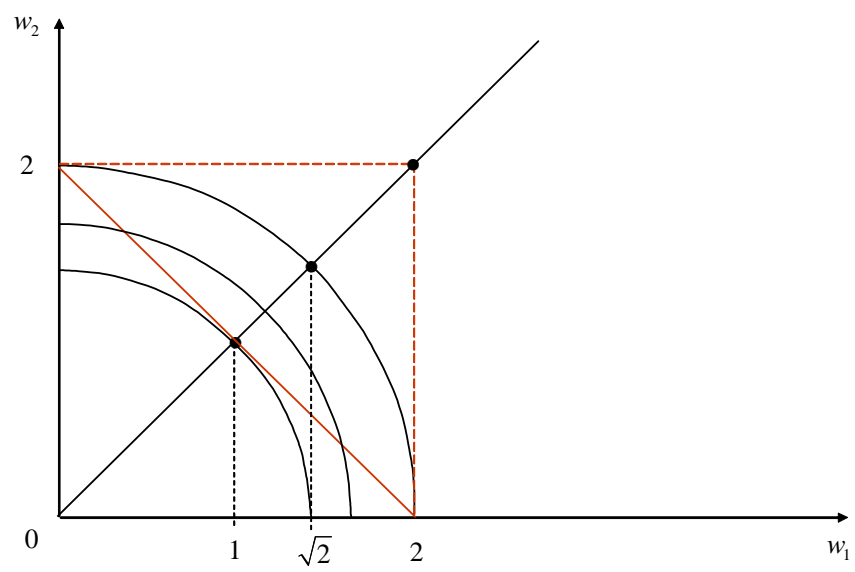


Figure 1: Illustration with quasi linear preferences and quadratic disutility of labor.

$(0, 2)$, while wage equalization $w_1 = w_2 = 1$ yields $S = 1$ (a local minimum). To achieve $S = 2$ under wage equalization one would need $(w_1, w_2) = (\sqrt{2}, \sqrt{2})$, which implies $w_1 + w_2 = 2\sqrt{2} > 2$. Consequently, to reach the same welfare with equal wages as with unequal wage distribution and lump-sum taxes, we need a larger total level of human capital.⁹

The level of (per capita) welfare as a function of w_2 , with $w_1 = 2 - w_2$ over the range $[1, 2]$ is represented on Figure 2. Not surprisingly this curve is monotonically increasing. Thus, whatever the level of \underline{w} the first-best solution always implies maximum wage differentiation. But of course this only confirms our theoretical results from Section 3.

We now turn to the second-best optimum. To tackle this problem we maximize (utilitarian) welfare for a given level of w_2 , with $w_1 = 2 - w_2$, subject to resource and self selection constraints. The resulting level of welfare is represented on Figure 2. Not surprisingly first- and second-best coincide for $w_1 = w_2 = 1$. From Proposition 2 we also expect them to coincide in the neighborhood of $w_2 = 2$ (i.e., $w_1 = 0$). The really interesting feature about this welfare profile is that the curve is not monotonic. This means that while a large wage differential (when allowed by the level of \underline{w}) is always better than wage equalization, small wage differentials may not be second-best optimal. In other words, when \underline{w} is large enough (more than roughly 0.8 in the example) wage equalization is effectively the second-best solution (and dominates $w_1 = \underline{w}$ and $w_2 = 2 - \underline{w}$). The orders of magnitude are of course of no relevance here but the illustration is sufficient to provide a counterexample and to show that a second-best solution with wage equalization can effectively arise.

Let us finally turn to the intuition behind this result. In the second-best, differentiating wages has two (contradictory) effects. First it is efficiency enhancing. This is shown by the fact the first best level of welfare is increasing in w_2 . However, it also brings in an informational problem (unobservable types and the

⁹A larger level of “total” human capital with equal wage than under unequal wages would be possible with decreasing returns to education. See the concluding section.

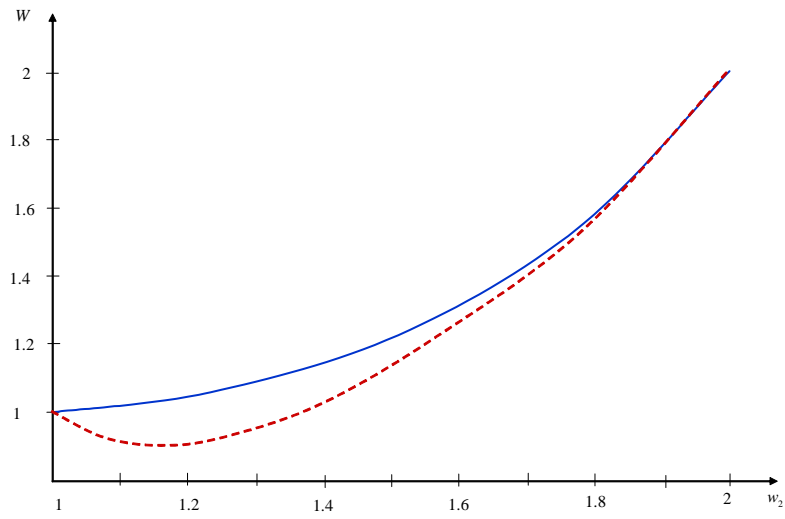


Figure 2: Welfare as a function of w_2 , with $w_1 = 2 - w_2$ at the first best (solid curve) and the second-best (dotted curve) solutions.

need for distortionary taxation). Interestingly this curve is also convex which mean that there are “increasing returns” to wage differentiation. Even though the shape of the curve is example specific, it is not surprising; recall the intuition behind Proposition 1 presented in Section 3. Because of these increasing returns the efficiency gain associated with a small wage differentiation is not sufficient to compensate for the adverse informational impact. However, a large degree of differentiation yields efficiency gains that outweigh the negative effects of information asymmetries.

6 Conclusion

When the productivities of otherwise identical individuals can be controlled through education expenses and when no subsequent redistribution through income taxation is available, it is clear the equal wage solution is very compelling. The question raised in this paper is different. We have studied the optimal distribution of productivity under the assumption that redistribution through an optimal income tax is also available. To give the equal wage outcome the best chance to emerge, we have also assumed that individuals have identical learning abilities. Nevertheless, it turns out that in the first-best inequality is always preferable to equality. In the second-best this conclusion has to be qualified. It only holds if the lower limit on productivity is not too high. Either way, the underlying problem is inherently non convex and a simple inspection of first-order conditions can be very misleading.

Admittedly, our model is at odds with most models of education. We assume that all individuals are ex ante identical; we also assume away the idea that educational spending has decreasing returns and the fact that the total amount of expenditure is endogenous. Let us see what would be the implications of relaxing these three assumptions. Making educational spending endogenous (and not equal to 2) would not change the main result. Decreasing returns could make a difference. Assume for the sake of illustration that instead of $w_1 + w_2 = 2$ we have

$\max(w_1, w_2) = 2$, then it is clear that social optimality would imply $w_1 = w_2$; see Figure 1. This illustration also makes it clear that the degree of decreasing returns to scale must be sufficiently strong to reverse our result. When the set of feasible wages is convex but with a frontier sufficiently close to the line representing $w_1 + w_2 = 2$ wages differentiation continues to be optimal. Roughly speaking the result is only reversed if the degree of concavity of the wage frontier is so large that its intersection with the 45 degree line is above the point $(\sqrt{2}, \sqrt{2})$. Finally, there is the assumption of uniform learning ability. If we were to assume different learning ability, then our results could only be strengthened. The main difference is that the individual with the higher wage level would be the more able.

To sum up, the somehow surprising result obtained in this paper is not just a technical curiosity, but would continue to hold in a more general class of setting. This calls for a number of remarks. First, it means that for people who are only concerned by the maximization of utilitarian social welfare the concept of “equality of opportunity”, defined as equality of earning capacity, might be undesirable.

Second, one may find unsatisfactory a society that achieves full equality of utilities, but consist of a majority of individuals without education. If we think that education brings utility by itself and thus should be explicitly introduced in the utility function, our conclusion would be different. Finally, we have to keep in mind that for reasons pertaining to political economy redistribution through education may be easier than tax redistribution.

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